

## **BIPOLAR INTERVAL VALUED INTUITIONISTIC FUZZY NECESSITY OPERATOR**

**M.Suganya<sup>[1]</sup>,A.Manonmani<sup>[2]</sup>**

<sup>[1]</sup>Research Scholar, Department of Mathematics, LRG Government Arts college for Women, Tirupur.

<sup>[2]</sup>Assistant Professor, Department of Mathematics, LRG Government Arts college for Women, Tirupur.

### **Abstract**

In this paper we have introduced the necessity operator on a Bipolar Interval Valued Intuitionistic Fuzzy Subset of a Bipolar Interval Valued Intuitionistic Fuzzy Topological space and verified its property.

### **Keyword**

Bipolar Interval Valued Intuitionistic Fuzzy Topological Space, Bipolar Interval Valued Intuitionistic Fuzzy Set.

### **1. Introduction:**

Lee introduced the concept of Bipolar fuzzy set. In Bipolar Intuitionistic Fuzzy Topology the membership and non-membership degree of the fuzzy set lies in the range [0,1] and [-1,0][21]. In this paper we have introduced the Bipolar Interval Valued Intuitionistic Fuzzy necessity operator on a Bipolar Interval Valued Intuitionistic Fuzzy Subset of a Bipolar Interval Valued Intuitionistic Fuzzy Topological space and verified that the necessity operator on a Bipolar Interval Valued Intuitionistic Fuzzy Subset itself forms a Bipolar Interval Valued Intuitionistic Fuzzy Topological space.

### **2. Definition:**

Let X be a non-empty set, and let A be a Bipolar interval valued intuitionistic fuzzy set on a Bipolar Interval Valued Intuitionistic Topological Space BIVIFTS(X), then the necessity operator on A is defined as

$$\text{i. } [ ]_A = \left\{ \left\langle x, \left[ \mu_{AL}^P(x), \mu_{AU}^P(x) \right], \left[ 1 - \mu_{AU}^P(x), 1 - \mu_{AL}^P(x) \right] \right\rangle \middle| x \in X \right\}$$

$$\quad \quad \quad \left[ \mu_{AL}^N(x), \mu_{AU}^N(x) \right], \left[ -1 + \mu_{AU}^N(x), -1 + \mu_{AL}^N(x) \right]$$

### **2.1. Theorem:**

Let  $(X, \tau)$  be a Bipolar Interval Valued Intuitionistic Fuzzy Topological Space (BIVIFTS). Based on the necessity operator on a Bipolar Interval Valued Intuitionistic Fuzzy set A on X, we can also construct several BIVIFTSs on X as

$$\tau_N = \{ [ ]A \mid A \in \tau \}$$

i.e., the necessity operator defined in the above definition itself forms a topology.

### **Proof:**

In order to prove the topology we have to prove the following

Let S be a set and  $\tau$  be a family of bipolar interval valued intuitionistic fuzzy subset of S. The family  $\tau$  is called a Bipolar Interval Valued Intuitionistic Fuzzy Topology (BIVIFT) on S if  $\tau$  satisfies the following axioms

i.  $0_s, 1_s \in \tau$

ii. If  $\{A_i; i \in I\} \subseteq \tau$ , then  $\bigcup_{i=1}^{\infty} A_i \in \tau$

iii. If  $A_1, A_2, A_3, \dots, A_n \in \tau$ , then  $\bigcap_{i=1}^n A_i \in \tau$

Let  $A_1, A_2, \dots, A_n$  be Bipolar interval valued intuitionistic fuzzy subsets on a Bipolar Interval Valued Intuitionistic Topological Space BIVIFTS(X).

To prove necessity operator is a Bipolar Interval Valued Intuitionistic Topological Space BIVIFTS(X)

i. obviously  $0_s, 1_s \in \tau_N$

ii.

$$A \cup B = \left\{ \left\langle x, \left[ \mu_{(A \cup B)L}^p(x), \mu_{(A \cup B)U}^p(x) \right], \left[ \mu_{(A \cap B)L}^N(x), \mu_{(A \cap B)U}^N(x) \right] \right\rangle \middle| x \in X \right\}$$

$$\left[ \gamma_{(A \cup B)L}^p(x), \gamma_{(A \cup B)U}^p(x) \right], \left[ \gamma_{(A \cap B)L}^N(x), \gamma_{(A \cap B)U}^N(x) \right]$$

where

$$\mu_{(A \cup B)L}^p(x) = \min \{ \mu_{AL}^p(x), \mu_{BL}^p(x) \}$$

$$\begin{aligned}
\mu_{(A \cup B)U}^p(x) &= \max \{\mu_{AU}^p(x), \mu_{BU}^p(x)\} \\
\mu_{(A \cap B)L}^N(x) &= \max \{\mu_{AL}^N(x), \mu_{BL}^N(x)\} \\
\mu_{(A \cap B)U}^N(x) &= \min \{\mu_{AU}^N(x), \mu_{BU}^N(x)\} \\
\gamma_{(A \cup B)L}^p(x) &= \min \{\gamma_{AL}^p(x), \gamma_{BL}^p(x)\} \\
\gamma_{(A \cup B)U}^p(x) &= \max \{\gamma_{AU}^p(x), \gamma_{BU}^p(x)\} \\
\gamma_{(A \cap B)L}^N(x) &= \max \{\gamma_{AL}^N(x), \gamma_{BL}^N(x)\} \\
\gamma_{(A \cap B)U}^N(x) &= \min \{\gamma_{AU}^N(x), \gamma_{BU}^N(x)\} \\
\Rightarrow [ ]_{A_1} \cup [ ]_{A_2} &= \left\{ \begin{array}{l} \left\langle x, \left[ \mu_{([ ]_{A_1} \cup [ ]_{A_2})L}^p(x), \mu_{([ ]_{A_1} \cup [ ]_{A_2})U}^p(x) \right] \right\rangle \\ \left[ \mu_{([ ]_{A_1} \cap [ ]_{A_2})L}^N(x), \mu_{([ ]_{A_1} \cap [ ]_{A_2})U}^N(x) \right] \\ \left[ \gamma_{([ ]_{A_1} \cup [ ]_{A_2})L}^p(x), \gamma_{([ ]_{A_1} \cup [ ]_{A_2})U}^p(x) \right] \\ \left[ \gamma_{([ ]_{A_1} \cap [ ]_{A_2})L}^N(x), \gamma_{([ ]_{A_1} \cap [ ]_{A_2})U}^N(x) \right] \end{array} \mid x \in X \right\}
\end{aligned}$$

where

$$\begin{aligned}
\mu_{([ ]_{A_1} \cup [ ]_{A_2})L}^p(x) &= \min \{\mu_{[ ]_{A_1} L}^p(x), \mu_{[ ]_{A_2} L}^p(x)\} \\
\mu_{([ ]_{A_1} \cup [ ]_{A_2})U}^p(x) &= \max \{\mu_{[ ]_{A_1} U}^p(x), \mu_{[ ]_{A_2} U}^p(x)\} \\
\mu_{([ ]_{A_1} \cap [ ]_{A_2})L}^N(x) &= \max \{\mu_{[ ]_{A_1} L}^N(x), \mu_{[ ]_{A_2} L}^N(x)\} \\
\mu_{([ ]_{A_1} \cap [ ]_{A_2})U}^N(x) &= \min \{\mu_{[ ]_{A_1} U}^N(x), \mu_{[ ]_{A_2} U}^N(x)\} \\
\gamma_{([ ]_{A_1} \cup [ ]_{A_2})L}^p(x) &= \min \{\gamma_{[ ]_{A_1} L}^p(x), \gamma_{[ ]_{A_2} L}^p(x)\} \\
\gamma_{([ ]_{A_1} \cup [ ]_{A_2})U}^p(x) &= \max \{\gamma_{[ ]_{A_1} U}^p(x), \gamma_{[ ]_{A_2} U}^p(x)\} \\
\gamma_{([ ]_{A_1} \cap [ ]_{A_2})L}^N(x) &= \max \{\gamma_{[ ]_{A_1} L}^N(x), \gamma_{[ ]_{A_2} L}^N(x)\} \\
\gamma_{([ ]_{A_1} \cap [ ]_{A_2})U}^N(x) &= \min \{\gamma_{[ ]_{A_1} U}^N(x), \gamma_{[ ]_{A_2} U}^N(x)\}
\end{aligned}$$

then

$$\begin{aligned}
\mu_{([ ]_{A_1} \cup [ ]_{A_2})L}^p(x) &= \min \{\mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x)\} \\
\mu_{([ ]_{A_1} \cup [ ]_{A_2})U}^p(x) &= \max \{\mu_{A_1 U}^p(x), \mu_{A_2 U}^p(x)\} \\
\mu_{([ ]_{A_1} \cap [ ]_{A_2})L}^N(x) &= \max \{\mu_{A_1 L}^N(x), \mu_{A_2 L}^N(x)\}
\end{aligned}$$

$$\begin{aligned}
& \mu_{(\ ]A_1 \cap [ ]A_2)_U}^N(x) = \min \{ \mu_{A_1 U}^N(x), \mu_{A_2 U}^N(x) \} \\
& 1 - \mu_{(\ ]A_1 \cup [ ]A_2)_L}^p(x) = \min \{ 1 - \mu_{A_1 L}^p(x), 1 - \mu_{A_2 L}^p(x) \} \\
& 1 - \mu_{(\ ]A_1 \cup [ ]A_2)_U}^p(x) = \max \{ 1 - \mu_{A_1 U}^p(x), 1 - \mu_{A_2 U}^p(x) \} \\
& 1 - \mu_{(\ ]A_1 \cap [ ]A_2)_L}^N(x) = \max \{ 1 - \mu_{A_1 L}^N(x), 1 - \mu_{A_2 L}^N(x) \} \\
& 1 - \mu_{(\ ]A_1 \cap [ ]A_2)_U}^N(x) = \min \{ 1 - \mu_{A_1 U}^N(x), 1 - \mu_{A_2 U}^N(x) \} \\
\\
& \Rightarrow [ ]A_1 \cup [ ]A_2 = \left\{ \begin{array}{l} x, [\mu_{(\ ]A_1 \cup [ ]A_2)_L}^p(x), \mu_{(\ ]A_1 \cup [ ]A_2)_U}^p(x)], \\ [\mu_{(\ ]A_1 \cap [ ]A_2)_L}^N(x), \mu_{(\ ]A_1 \cap [ ]A_2)_U}^N(x)], \\ [1 - \mu_{(\ ]A_1 \cup [ ]A_2)_L}^p(x), 1 - \mu_{(\ ]A_1 \cup [ ]A_2)_U}^p(x)], \\ [1 - \mu_{(\ ]A_1 \cap [ ]A_2)_L}^N(x), 1 - \mu_{(\ ]A_1 \cap [ ]A_2)_U}^N(x)] \end{array} \right| x \in X \in \tau_N \\
\\
& \Rightarrow [ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i = \left\{ \begin{array}{l} x, [\mu_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_L}^p(x), \mu_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_U}^p(x)], \\ [\mu_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_L}^N(x), \mu_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_U}^N(x)], \\ [\gamma_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_L}^p(x), \gamma_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_U}^p(x)], \\ [\gamma_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_L}^N(x), \gamma_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_U}^N(x)] \end{array} \right| x \in X \}
\end{aligned}$$

where

$$\begin{aligned}
& \mu_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_L}^p(x) = \min \{ \mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x), \dots, \mu_{A_i L}^p(x) \} \\
& \mu_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_U}^p(x) = \max \{ \mu_{A_1 U}^p(x), \mu_{A_2 U}^p(x), \dots, \mu_{A_i U}^p(x) \} \\
& \mu_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_L}^N(x) = \max \{ \mu_{A_1 L}^N(x), \mu_{A_2 L}^N(x), \dots, \mu_{A_i L}^N(x) \} \\
& \mu_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_U}^N(x) = \min \{ \mu_{A_1 U}^N(x), \mu_{A_2 U}^N(x), \dots, \mu_{A_i U}^N(x) \} \\
& \gamma_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_L}^p(x) = \min \{ \gamma_{A_1 L}^p(x), \gamma_{A_2 L}^p(x), \dots, \gamma_{A_i L}^p(x) \} \\
& \gamma_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_U}^p(x) = \max \{ \gamma_{A_1 U}^p(x), \gamma_{A_2 U}^p(x), \dots, \gamma_{A_i U}^p(x) \} \\
& \gamma_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_L}^N(x) = \max \{ \gamma_{A_1 L}^N(x), \gamma_{A_2 L}^N(x), \dots, \gamma_{A_i L}^N(x) \} \\
& \gamma_{(\ ]A_1 \cap [ ]A_2 \cap \dots \cap [ ]A_i)_U}^N(x) = \min \{ \gamma_{A_1 U}^N(x), \gamma_{A_2 U}^N(x), \dots, \gamma_{A_i U}^N(x) \}
\end{aligned}$$

then

$$\mu_{(\ ]A_1 \cup [ ]A_2 \cup \dots \cup [ ]A_i)_L}^p(x) = \min \{ \mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x), \dots, \mu_{A_i L}^p(x) \}$$

$$\begin{aligned}
& \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_U])}^p(x) = \max \{\mu_{A_1}^p(x), \mu_{A_2}^p(x), \dots, \mu_{A_i}^p(x)\} \\
& \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_L])}^N(x) = \max \{\mu_{A_1}^N(x), \mu_{A_2}^N(x), \dots, \mu_{A_i}^N(x)\} \\
& \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_U])}^N(x) = \min \{\mu_{A_1}^N(x), \mu_{A_2}^N(x), \dots, \mu_{A_i}^N(x)\} \\
& 1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_L])}^p(x) = \min \{1 - \mu_{A_1}^p(x), 1 - \mu_{A_2}^p(x), \dots, 1 - \mu_{A_i}^p(x)\} \\
& 1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_U])}^p(x) = \max \{1 - \mu_{A_1}^p(x), 1 - \mu_{A_2}^p(x), \dots, 1 - \mu_{A_i}^p(x)\} \\
& 1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_L])}^N(x) = \max \{1 - \mu_{A_1}^N(x), 1 - \mu_{A_2}^N(x), \dots, 1 - \mu_{A_i}^N(x)\} \\
& 1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_U])}^N(x) = \min \{1 - \mu_{A_1}^N(x), 1 - \mu_{A_2}^N(x), \dots, 1 - \mu_{A_i}^N(x)\} \\
& \Rightarrow [A_1 \cup [A_2 \cup \dots [A_i] = \left\{ \begin{array}{l} x, [\mu_{([A_1 \cup [A_2 \cup \dots [A_i]_L])}^p(x), \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_U])}^p(x)], \\ [\mu_{([A_1 \cap [A_2 \cap \dots [A_i]_L])}^N(x), \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_U])}^N(x)], \\ [1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_L])}^p(x), 1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i]_U])}^p(x)], \\ [1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_L])}^N(x), 1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i]_U])}^N(x)] \end{array} \right\} | x \in X \in \tau_N
\end{aligned}$$

Hence the arbitrary union of Bipolar Interval Valued Intuitionistic Necessity Operators is in Bipolar Interval Valued Intuitionistic Fuzzy Topology  $\tau$ .

iii.

$$A \cap B = \left\{ \left\langle x, \left[ \mu_{(A \cap B)L}^p(x), \mu_{(A \cap B)U}^p(x) \right], \left[ \mu_{(A \cap B)L}^N(x), \mu_{(A \cap B)U}^N(x) \right] \right\rangle \mid x \in X \right\}$$

where

$$\mu_{(A \cap B)L}^p(x) = \max \{\mu_{AL}^p(x), \mu_{BL}^p(x)\}$$

$$\mu_{(A \cap B)U}^p(x) = \min \{\mu_{AU}^p(x), \mu_{BU}^p(x)\}$$

$$\mu_{(A \cap B)L}^N(x) = \min \{\mu_{AL}^N(x), \mu_{BL}^N(x)\}$$

$$\mu_{(A \cap B)U}^N(x) = \max \{\mu_{AU}^N(x), \mu_{BU}^N(x)\}$$

$$\gamma_{(A \cap B)L}^p(x) = \max \{\gamma_{AL}^p(x), \gamma_{BL}^p(x)\}$$

$$\gamma_{(A \cap B)U}^p(x) = \min \{\gamma_{AU}^p(x), \gamma_{BU}^p(x)\}$$

$$\gamma_{(A \cap B)L}^N(x) = \min \{\gamma_{AL}^N(x), \gamma_{BL}^N(x)\}$$

$$\gamma_{(A \cup B)U}^N(x) = \max \{\gamma_{AU}^N(x), \gamma_{BU}^N(x)\}$$

then

$$(A_1 \cap A_2) = \left\{ \begin{array}{l} \left\langle x, [\mu_{[A_1 \cap A_2]L}^p(x), \mu_{[A_1 \cap A_2]U}^p(x)] \right\rangle \\ \left\langle [\mu_{[A_1 \cup A_2]L}^N(x), \mu_{[A_1 \cup A_2]U}^N(x)] \right\rangle \\ \left\langle [\gamma_{[A_1 \cap A_2]L}^p(x), \gamma_{[A_1 \cap A_2]U}^p(x)] \right\rangle \\ \left\langle [\gamma_{[A_1 \cup A_2]L}^N(x), \gamma_{[A_1 \cup A_2]U}^N(x)] \right\rangle \end{array} \mid x \in X \right\}$$

where

$$\begin{aligned} \mu_{[A_1 \cap A_2]L}^p(x) &= \max \{\mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x)\} \\ \mu_{[A_1 \cap A_2]U}^p(x) &= \min \{\mu_{A_1 U}^p(x), \mu_{A_2 U}^p(x)\} \\ \mu_{[A_1 \cup A_2]L}^N(x) &= \min \{\mu_{A_1 L}^N(x), \mu_{A_2 L}^N(x)\} \\ \mu_{[A_1 \cup A_2]U}^N(x) &= \max \{\mu_{A_1 U}^N(x), \mu_{A_2 U}^N(x)\} \\ \gamma_{[A_1 \cap A_2]L}^p(x) &= \max \{\gamma_{A_1 L}^p(x), \gamma_{A_2 L}^p(x)\} \\ \gamma_{[A_1 \cap A_2]U}^p(x) &= \min \{\gamma_{A_1 U}^p(x), \gamma_{A_2 U}^p(x)\} \\ \gamma_{[A_1 \cup A_2]L}^N(x) &= \min \{\gamma_{A_1 L}^N(x), \gamma_{A_2 L}^N(x)\} \\ \gamma_{[A_1 \cup A_2]U}^N(x) &= \max \{\gamma_{A_1 U}^N(x), \gamma_{A_2 U}^N(x)\} \end{aligned}$$

then

$$\begin{aligned} \mu_{[A_1 \cap A_2]L}^p(x) &= \max \{\mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x)\} \\ \mu_{[A_1 \cap A_2]U}^p(x) &= \min \{\mu_{A_1 U}^p(x), \mu_{A_2 U}^p(x)\} \\ \mu_{[A_1 \cup A_2]L}^N(x) &= \min \{\mu_{A_1 L}^N(x), \mu_{A_2 L}^N(x)\} \\ \mu_{[A_1 \cup A_2]U}^N(x) &= \max \{\mu_{A_1 U}^N(x), \mu_{A_2 U}^N(x)\} \\ 1 - \mu_{[A_1 \cap A_2]L}^p(x) &= \max \{1 - \mu_{A_1 L}^p(x), 1 - \mu_{A_2 L}^p(x)\} \\ 1 - \mu_{[A_1 \cap A_2]U}^p(x) &= \min \{1 - \mu_{A_1 U}^p(x), 1 - \mu_{A_2 U}^p(x)\} \\ 1 - \mu_{[A_1 \cup A_2]L}^N(x) &= \min \{1 - \mu_{A_1 L}^N(x), 1 - \mu_{A_2 L}^N(x)\} \end{aligned}$$

$$1 - \mu_{([A_1 \cup [A_2]_U)}^N(x) = \max \{1 - \mu_{A_1 U}^N(x), 1 - \mu_{A_2 U}^N(x)\}$$

$$\Rightarrow [A_1 \cap [A_2] = \left\{ \begin{array}{l} \left[ x, [\mu_{([A_1 \cap [A_2]_L}^p(x), \mu_{([A_1 \cap [A_2]_U}^p(x)],, \right], \\ \left[ \mu_{([A_1 \cup [A_2]_L}^N(x), \mu_{([A_1 \cup [A_2]_U}^N(x)],, \right], \\ \left[ 1 - \mu_{([A_1 \cap [A_2]_L}^p(x), 1 - \mu_{([A_1 \cap [A_2]_U}^p(x)],, \right], \\ \left[ 1 - \mu_{([A_1 \cup [A_2]_L}^N(x), 1 - \mu_{([A_1 \cup [A_2]_U}^N(x)] \end{array} \right\} | x \in X \in \tau_N$$

$$\Rightarrow [A_1 \cap [A_2 \cap ... [A_i] = \left\{ \begin{array}{l} \left[ x, [\mu_{([A_1 \cap [A_2 \cap ... [A_i]_L}^p(x), \mu_{([A_1 \cap [A_2 \cap ... [A_i]_U}^p(x)],, \right], \\ \left[ \mu_{([A_1 \cup [A_2 \cup ... [A_i]_L}^N(x), \mu_{([A_1 \cup [A_2 \cup ... [A_i]_U}^N(x)],, \right], \\ \left[ \gamma_{([A_1 \cap [A_2 \cup ... [A_i]_L}^p(x), \gamma_{([A_1 \cap [A_2 \cup ... [A_i]_U}^p(x)],, \right], \\ \left[ \gamma_{([A_1 \cup [A_2 \cup ... [A_i]_L}^N(x), \gamma_{([A_1 \cup [A_2 \cup ... [A_i]_U}^N(x)] \end{array} \right\} | x \in X$$

where

$$\mu_{([A_1 \cap [A_2 \cap ... [A_i]_L}^p(x) = \max \{\mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x), ..., \mu_{A_i L}^p(x)\}$$

$$\mu_{([A_1 \cap [A_2 \cap ... [A_i]_U}^p(x) = \min \{\mu_{A_1 U}^p(x), \mu_{A_2 U}^p(x), ..., \mu_{A_i U}^p(x)\}$$

$$\mu_{([A_1 \cup [A_2 \cup ... [A_i]_L}^N(x) = \min \{\mu_{A_1 L}^N(x), \mu_{A_2 L}^N(x), ..., \mu_{A_i L}^N(x)\}$$

$$\mu_{([A_1 \cup [A_2 \cup ... [A_i]_U}^N(x) = \max \{\mu_{A_1 U}^N(x), \mu_{A_2 U}^N(x), ..., \mu_{A_i U}^N(x)\}$$

$$\gamma_{([A_1 \cap [A_2 \cup ... [A_i]_L}^p(x) = \max \{\gamma_{A_1 L}^p(x), \gamma_{A_2 L}^p(x), ..., \gamma_{A_i L}^p(x)\}$$

$$\gamma_{([A_1 \cap [A_2 \cup ... [A_i]_U}^p(x) = \min \{\gamma_{A_1 U}^p(x), \gamma_{A_2 U}^p(x), ..., \gamma_{A_i U}^p(x)\}$$

$$\gamma_{([A_1 \cup [A_2 \cup ... [A_i]_L}^N(x) = \min \{\gamma_{A_1 L}^N(x), \gamma_{A_2 L}^N(x), ..., \gamma_{A_i L}^N(x)\}$$

$$\gamma_{([A_1 \cup [A_2 \cup ... [A_i]_U}^N(x) = \max \{\gamma_{A_1 U}^N(x), \gamma_{A_2 U}^N(x), ..., \gamma_{A_i U}^N(x)\}$$

then

$$\mu_{([A_1 \cap [A_2 \cap ... [A_i]_L}^p(x) = \max \{\mu_{A_1 L}^p(x), \mu_{A_2 L}^p(x), ..., \mu_{A_i L}^p(x)\}$$

$$\mu_{([A_1 \cap [A_2 \cap \dots [A_i])U}^p(x) = \min \{ \mu_{A_{1U}}^p(x), \mu_{A_{2U}}^p(x), \dots, \mu_{A_{iU}}^p(x) \}$$

$$\mu_{([A_1 \cup [A_2 \cup \dots [A_i])L}^N(x) = \min \{ \mu_{A_{1L}}^N(x), \mu_{A_{2L}}^N(x), \dots, \mu_{A_{iL}}^N(x) \}$$

$$\mu_{([A_1 \cup [A_2 \cup \dots [A_i])U}^N(x) = \max \{ \mu_{A_{1U}}^N(x), \mu_{A_{2U}}^N(x), \dots, \mu_{A_{iU}}^N(x) \}$$

$$1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i])L}^p(x) = \max \{ 1 - \mu_{A_{1L}}^p(x), 1 - \mu_{A_{2L}}^p(x), \dots, 1 - \mu_{A_{iL}}^p(x) \}$$

$$1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i])U}^p(x) = \min \{ 1 - \mu_{A_{1U}}^p(x), 1 - \mu_{A_{2U}}^p(x), \dots, 1 - \mu_{A_{iU}}^p(x) \}$$

$$1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i])L}^N(x) = \min \{ 1 - \mu_{A_{1L}}^N(x), 1 - \mu_{A_{2L}}^N(x), \dots, 1 - \mu_{A_{iL}}^N(x) \}$$

$$1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i])U}^N(x) = \max \{ 1 - \mu_{A_{1U}}^N(x), 1 - \mu_{A_{2U}}^N(x), \dots, 1 - \mu_{A_{iU}}^N(x) \}$$

$$\Rightarrow [A_1 \cap [A_2 \cap \dots [A_i] = \left\{ \begin{array}{l} \left[ x, \left[ \mu_{([A_1 \cap [A_2 \cap \dots [A_i])L}^p(x), \mu_{([A_1 \cap [A_2 \cap \dots [A_i])U}^p(x) \right], \right. \\ \left. \left[ \mu_{([A_1 \cup [A_2 \cup \dots [A_i])L}^N(x), \mu_{([A_1 \cup [A_2 \cup \dots [A_i])U}^N(x) \right], \right. \\ \left. \left[ 1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i])L}^p(x), 1 - \mu_{([A_1 \cap [A_2 \cap \dots [A_i])U}^p(x) \right], \right. \\ \left. \left[ 1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i])L}^N(x), 1 - \mu_{([A_1 \cup [A_2 \cup \dots [A_i])U}^N(x) \right] \right] \end{array} \right| x \in X \in \tau_N$$

Hence the finite intersection of Bipolar Interval Valued Intuitionistic Necessity Operators is in Bipolar Interval Valued Intuitionistic Fuzzy Topology  $\tau$ .

Hence the Bipolar Interval Valued Intuitionistic Necessity Operators itself forms a Bipolar Interval Valued Intuitionistic Fuzzy Topology  $\tau$ .

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